

Correcting the ionosphere ➔



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Phase delay:

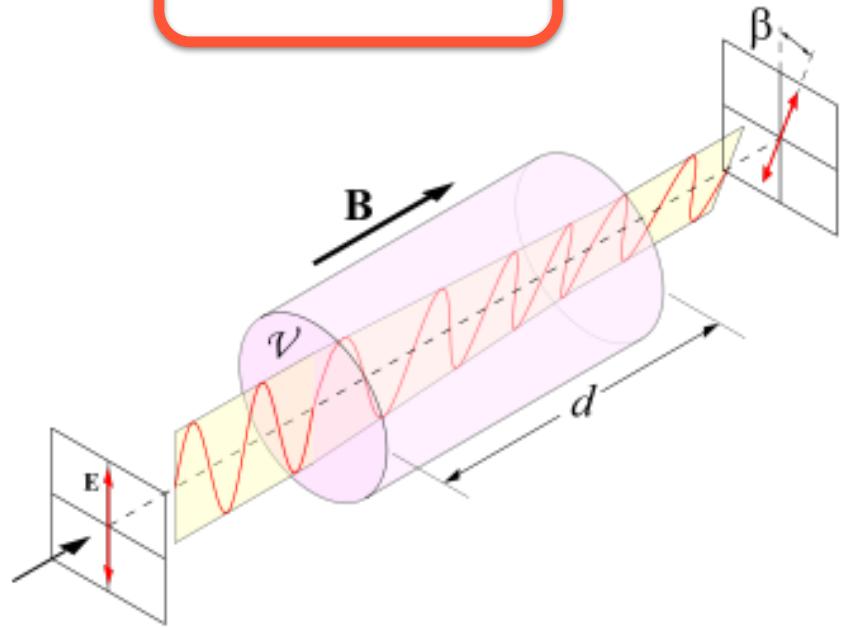
$$\phi_{\text{ion}} \approx \frac{e^2}{4\pi\epsilon_0 m \nu} \int_0^d n_e ds$$

Faraday rotation:

$$\beta = \text{RM} \nu^{-2}, \quad \text{RM} = \frac{e^3}{8\pi^2 \epsilon_0 m^2 c^3} \int_0^d n_e(s) B_{||}(s) ds$$

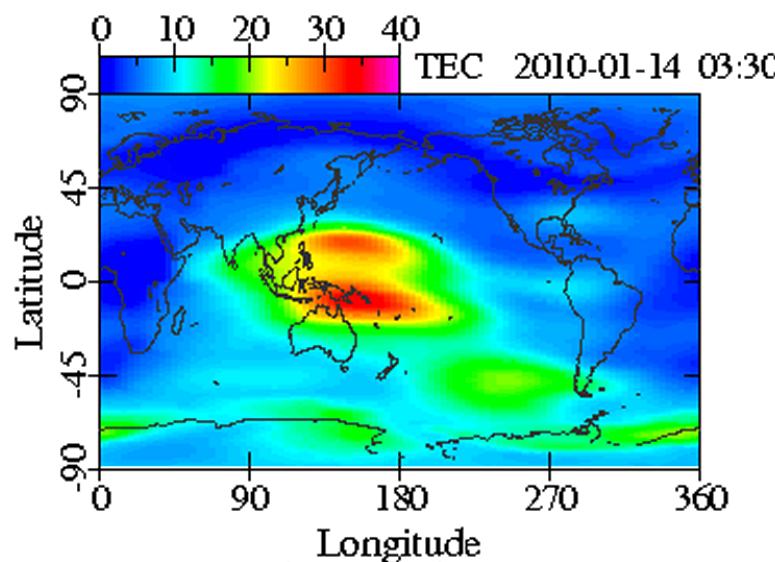
Ionosphere

- Partially **ionized** gas layer
- Permeated by Earth's **magnetic field**
- Mainly ionized by **Sun** through UV and short X-ray
- Strong **daily cycle**, annual cycle, solar activity cycle
- Free electron density is **variable in space-time**
- Typical vertical column density at night: $10^{16} \text{ m}^{-2} = 1 \text{ TECU}$

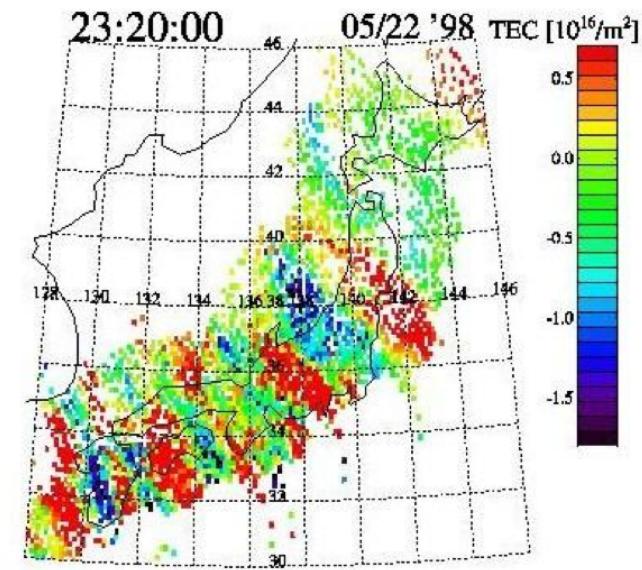


The ionosphere

- Large-scale variations:
 - ♦ TEC varying orders of magnitude
 - ♦ Cause: shift of the observing field



- Traveling Ionospheric Disturbances (TIDs):
 - ♦ 200 - 400 km height
 - ♦ 250 - 400 km wavelength
 - ♦ 300 - 700 km/h
 - ♦ 1 - 5% TEC variations
 - ♦ Cause: local source shift and distortions



Field of View

VLA 350 MHz
2°

VLA 1400 MHz
0.5°

GMRT 150 MHz
3°

LOFAR-HBA 140 MHz
4°

24 h cycle

LOFAR-LBA 60 MHz
10°

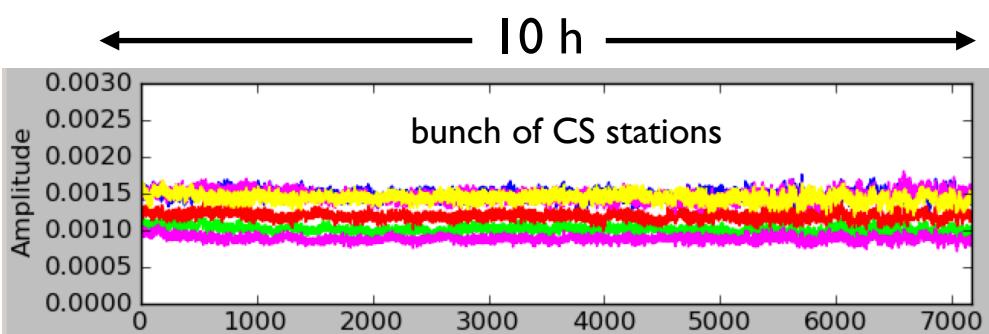
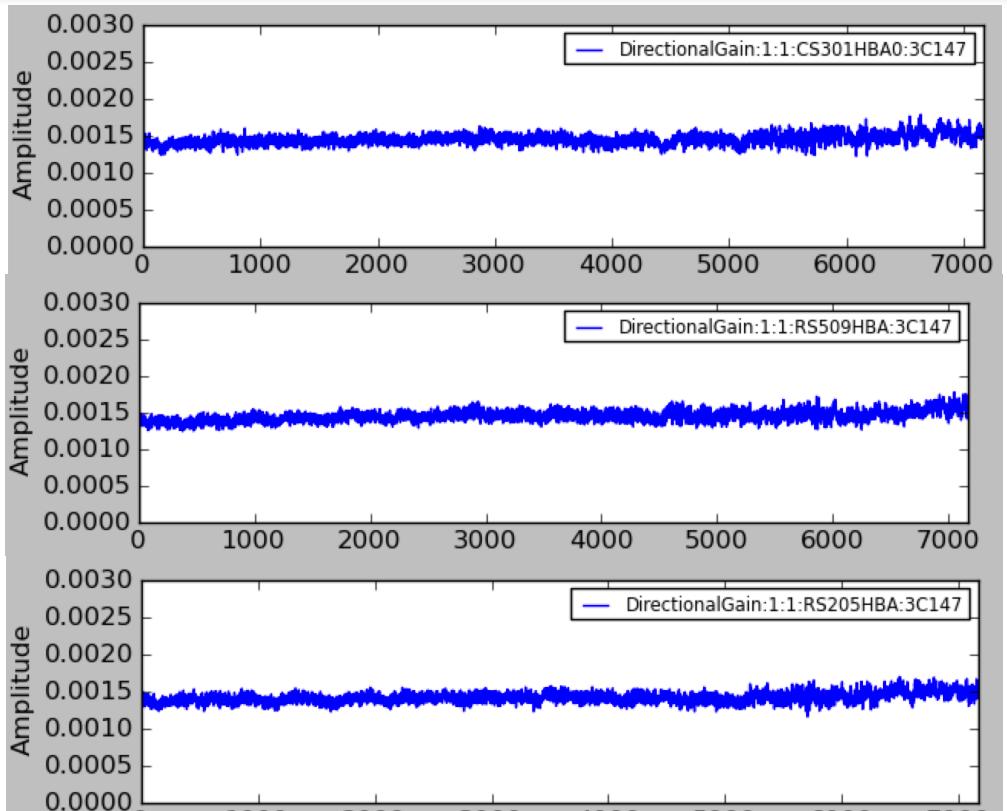
- Goal (Tier-I HBA):

- Noise level: ~100 microJy/beam with 10 h of data
- Resolution: ~5 arcsec
- Image quality (DR: 10^4 - 10^5)
- Reliable fluxes: < 5%

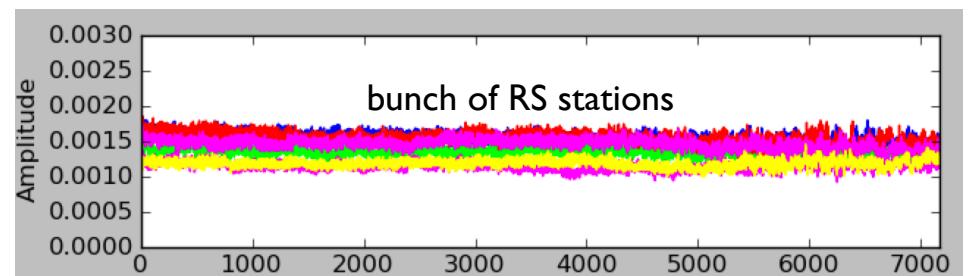
- Current status:

- No selfcal → few mJy noise (arcmin resolution)
- Selfcal → ~1 mJy “effective noise”, arcsec resolution
- HBA: no fundamental limitations in terms of S/N
- LBA: situation looks (much) more problematic

Calibrator stability



- ▶ Large elevation changes (40-90 deg)
- ▶ No time dependent gain corrections needed
- ▶ Single correction sufficient to get the amps calibrated
- ▶ We could just have observed 3C147/3C295/196 for ~30 min
- ▶ Variations that people report are likely calibration issues
 - A-team signal
 - not properly treating the field around the calibrator



Implementations

- **Extreme peeling** (van Weeren)

- Proven working (HBA)
- Slow (1 month/10h obs)
- User interaction

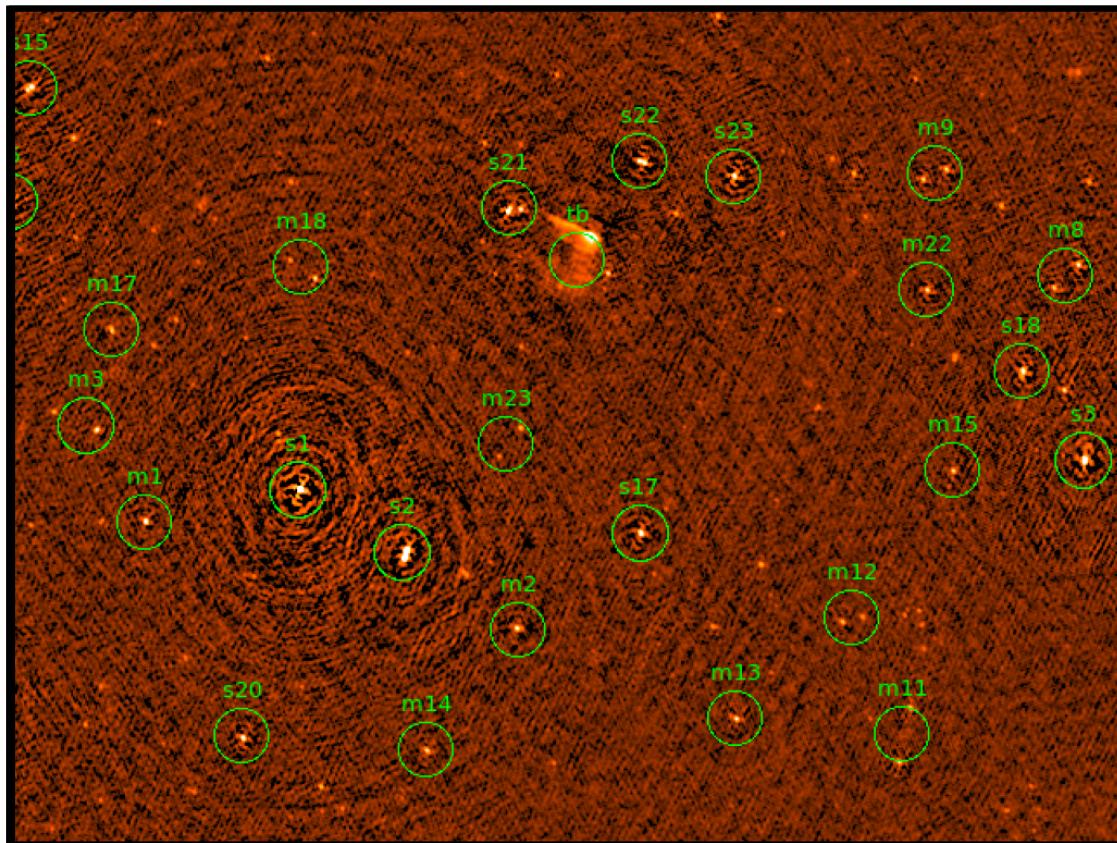
- **dTEC fitting** (Rafferty, van der Tol)

- Proven working (for LBA!)
- Slow
- Automated

- **CSPAM** (Intema, de Gasperin)

- Proven working
- Less slow
- Automated

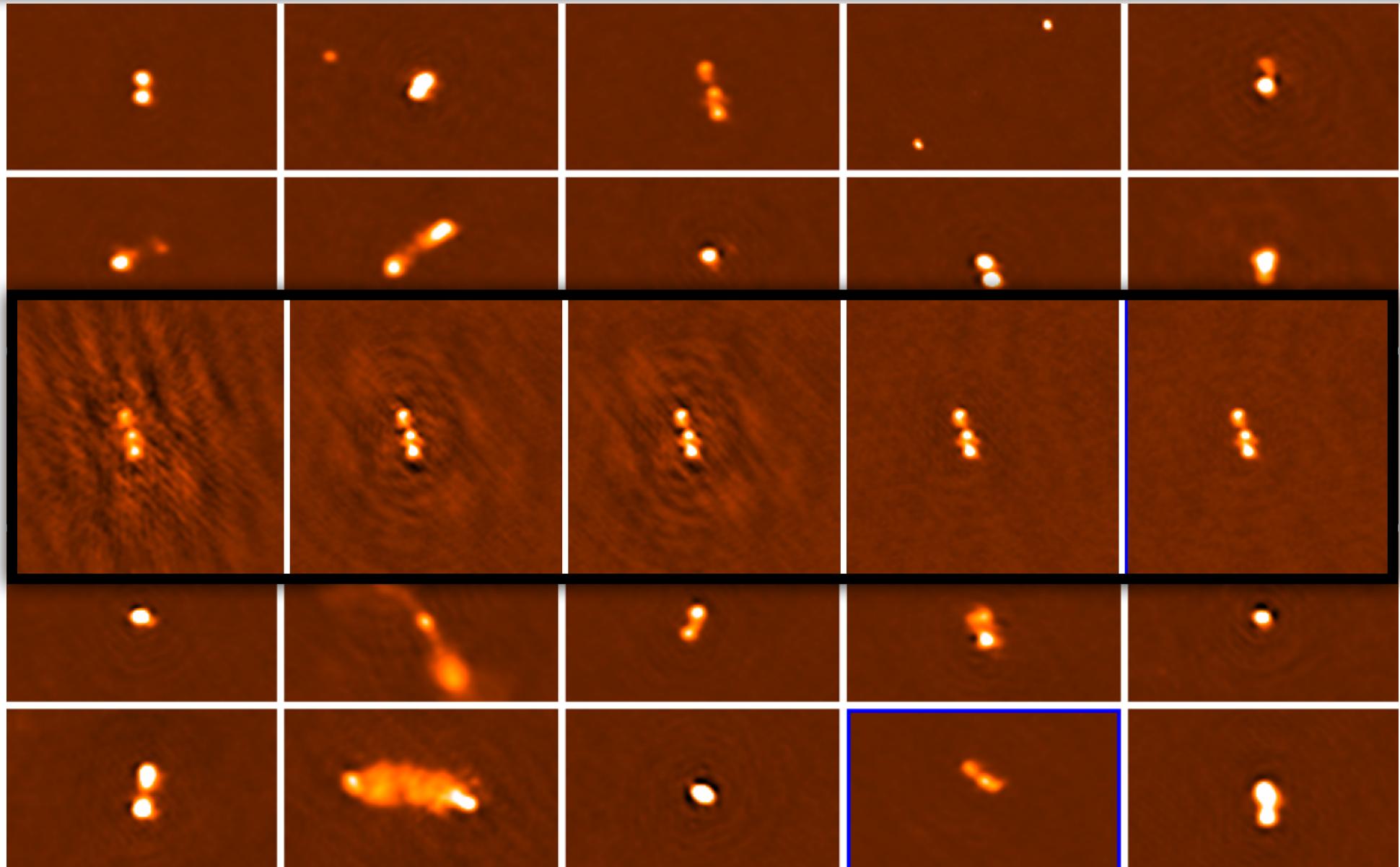
Extreme peeling: define directions



- iterate over directions for direction dependent calibration
- computing time simply scales with number of directions
- full selfcal+imaging cycle per direction (source models are updated all the time)

- All compact sources above ~ 0.1 Jy
- Bright extended sources
- Done manually

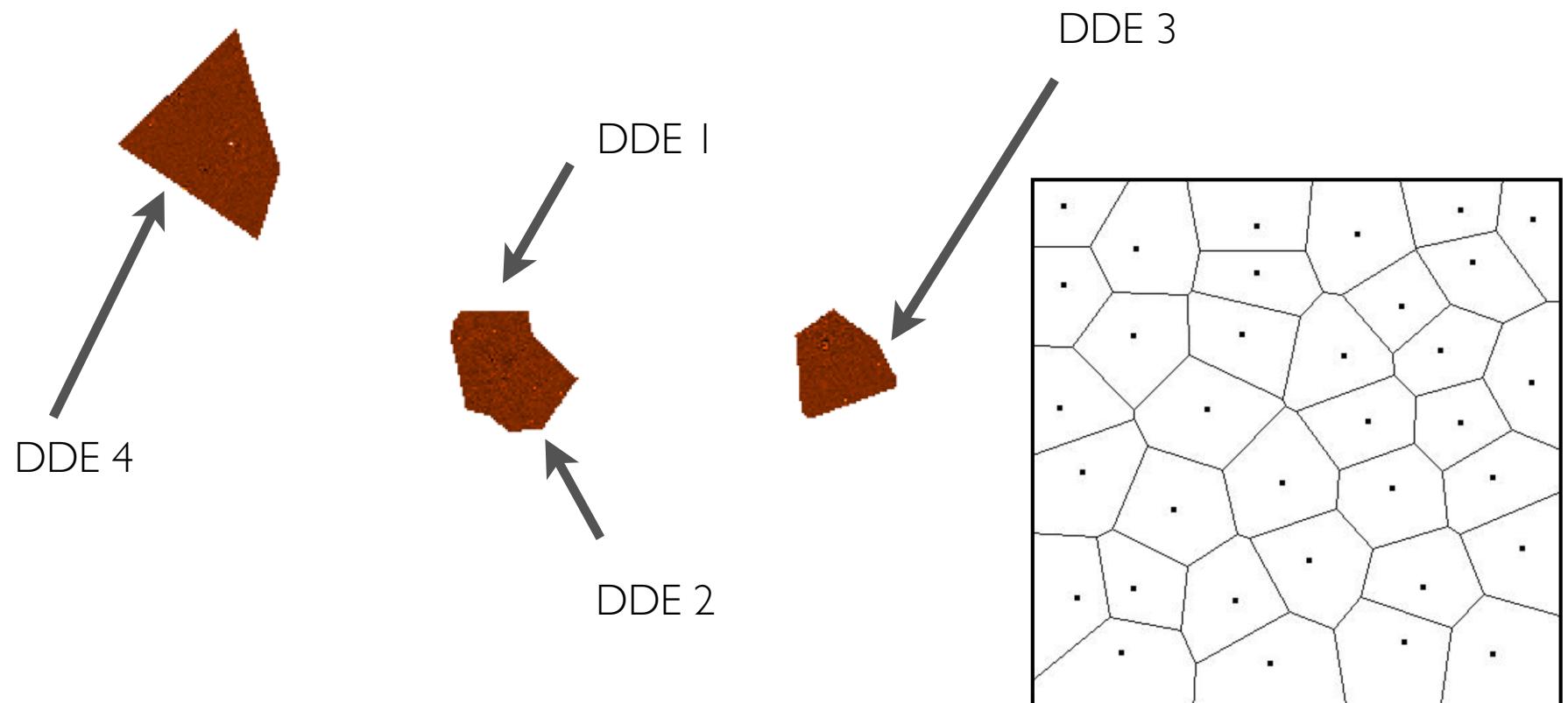
Tessellation



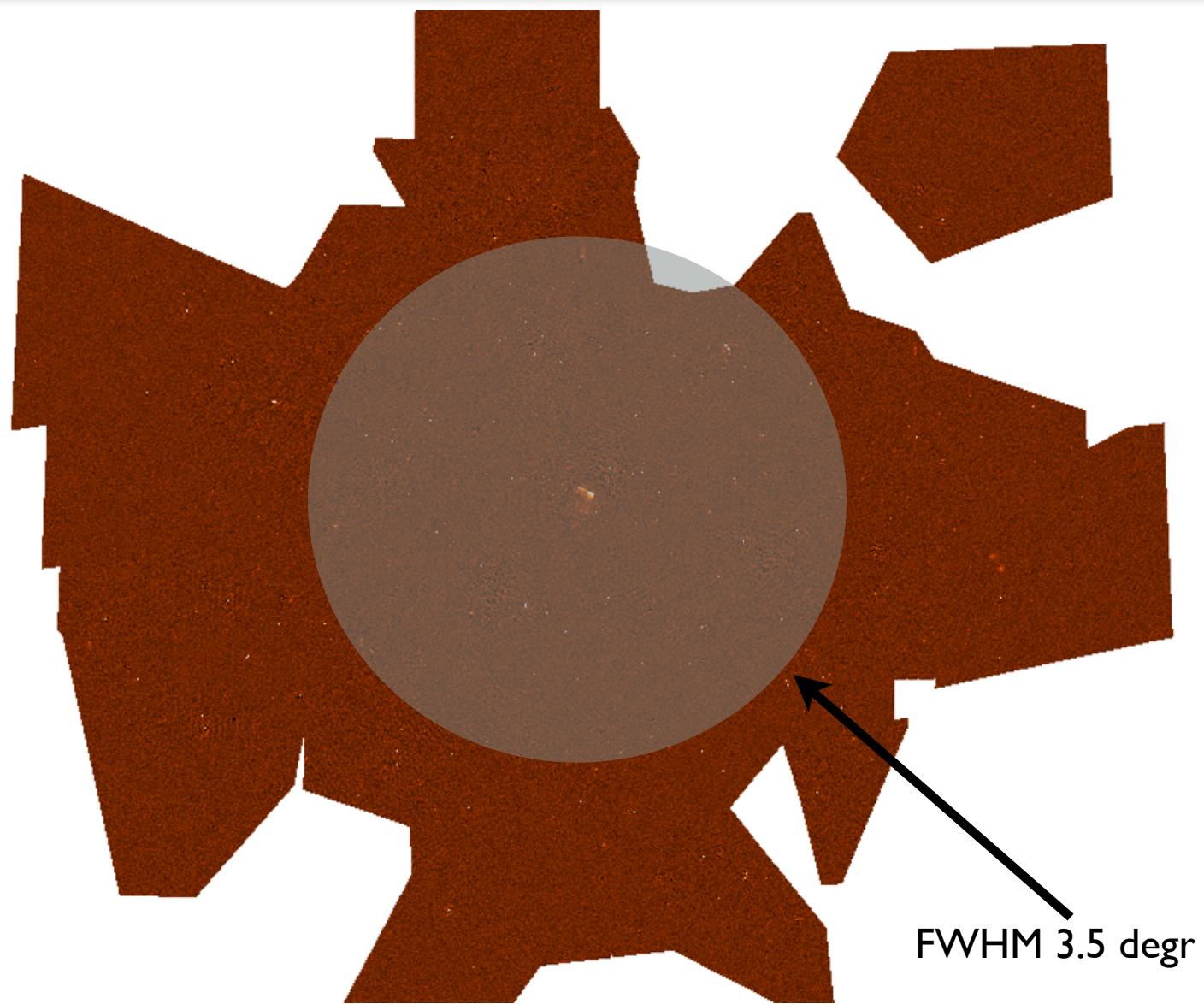
Tessellation

DD calibration:

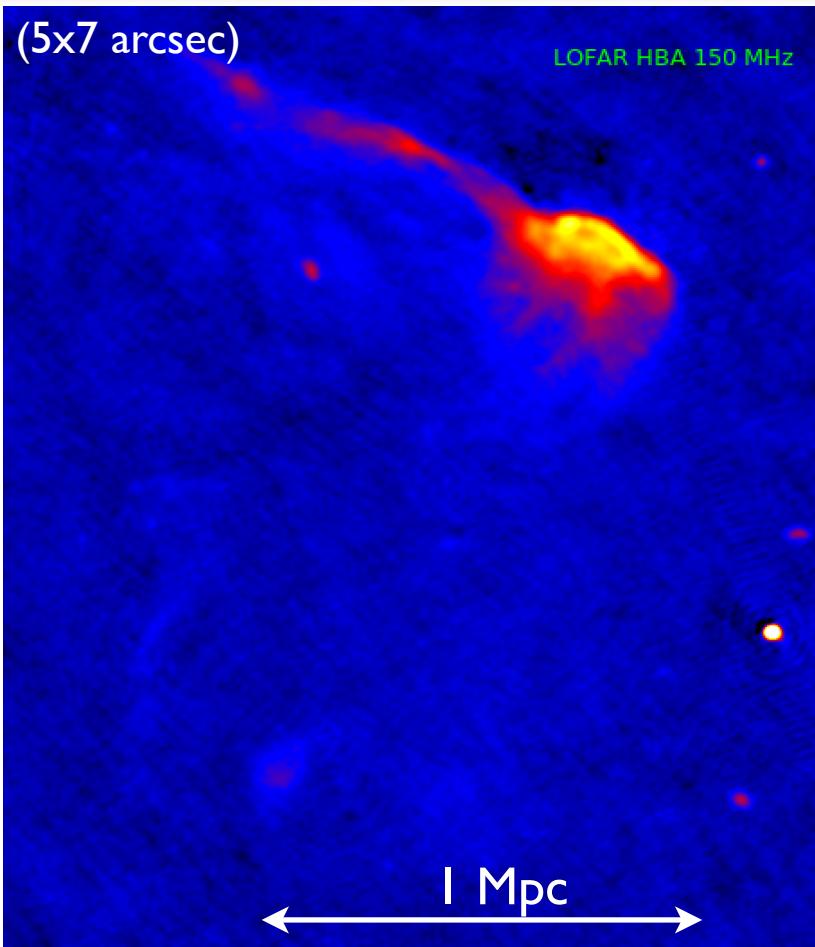
1. Add back one of the “peeling source”
2. Selfcal on the source for all SBs
3. Add the fainter sources back in the region around the peeling sources
4. Apply the DDE/peeling solution and image this part of the sky
5. Subtract the “updated model” from the original “residual datasets”



Result

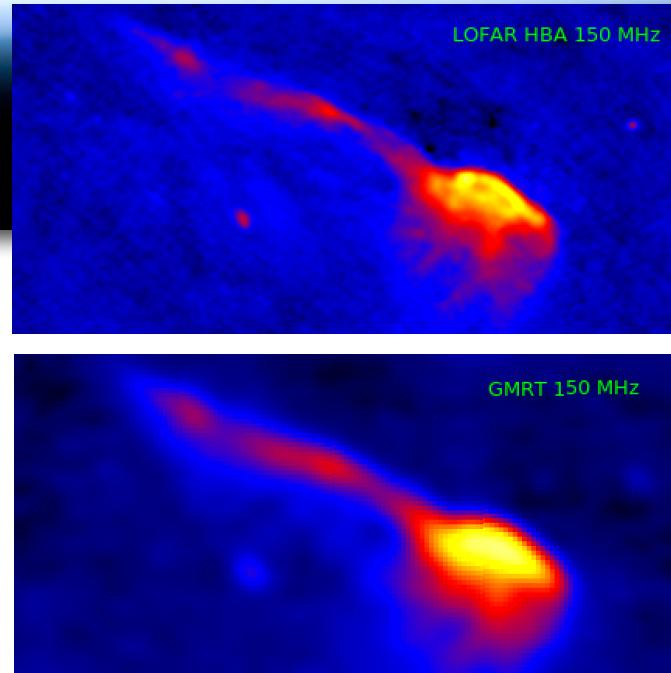


(courtesy of R. van Weeren)



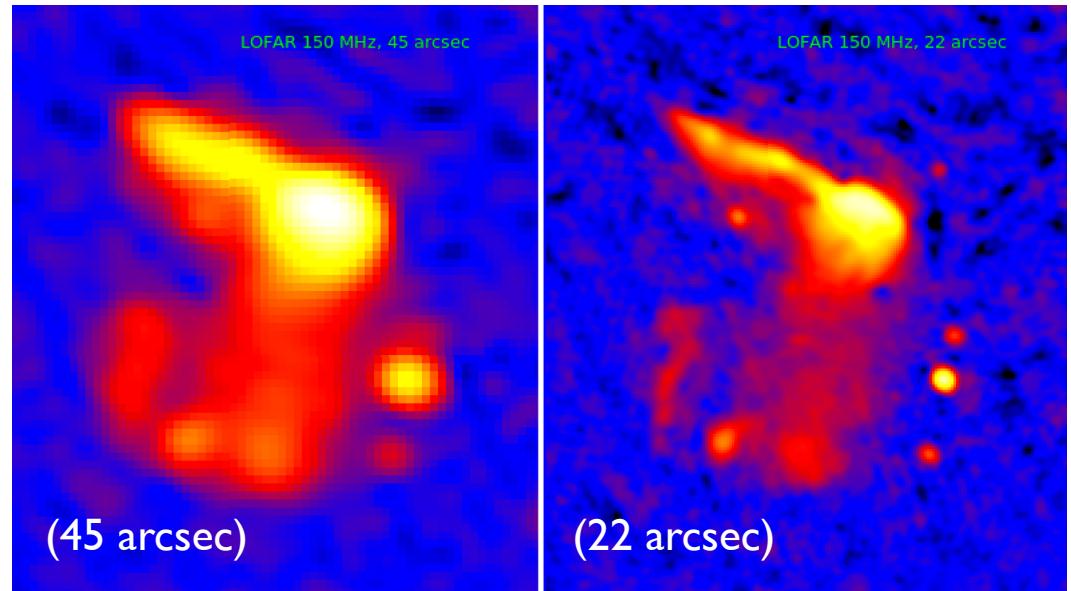
full resolution (5x7 arcsec), 140-160 MHz
close to thermal noise (190-250 microJy/beam)
only 30% of available bandwidth.....

LOFAR vs GMRT



Result

emphasize large-scale emission with weighting



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- Perform direction-dependent calibration for bright sources
- Assume that instrumental effects are the same in all directions for a given station:

Source 1:

$$\phi_1^{\text{cal}} = \phi^{\text{instr}} + \phi_1^{\text{ion}}$$

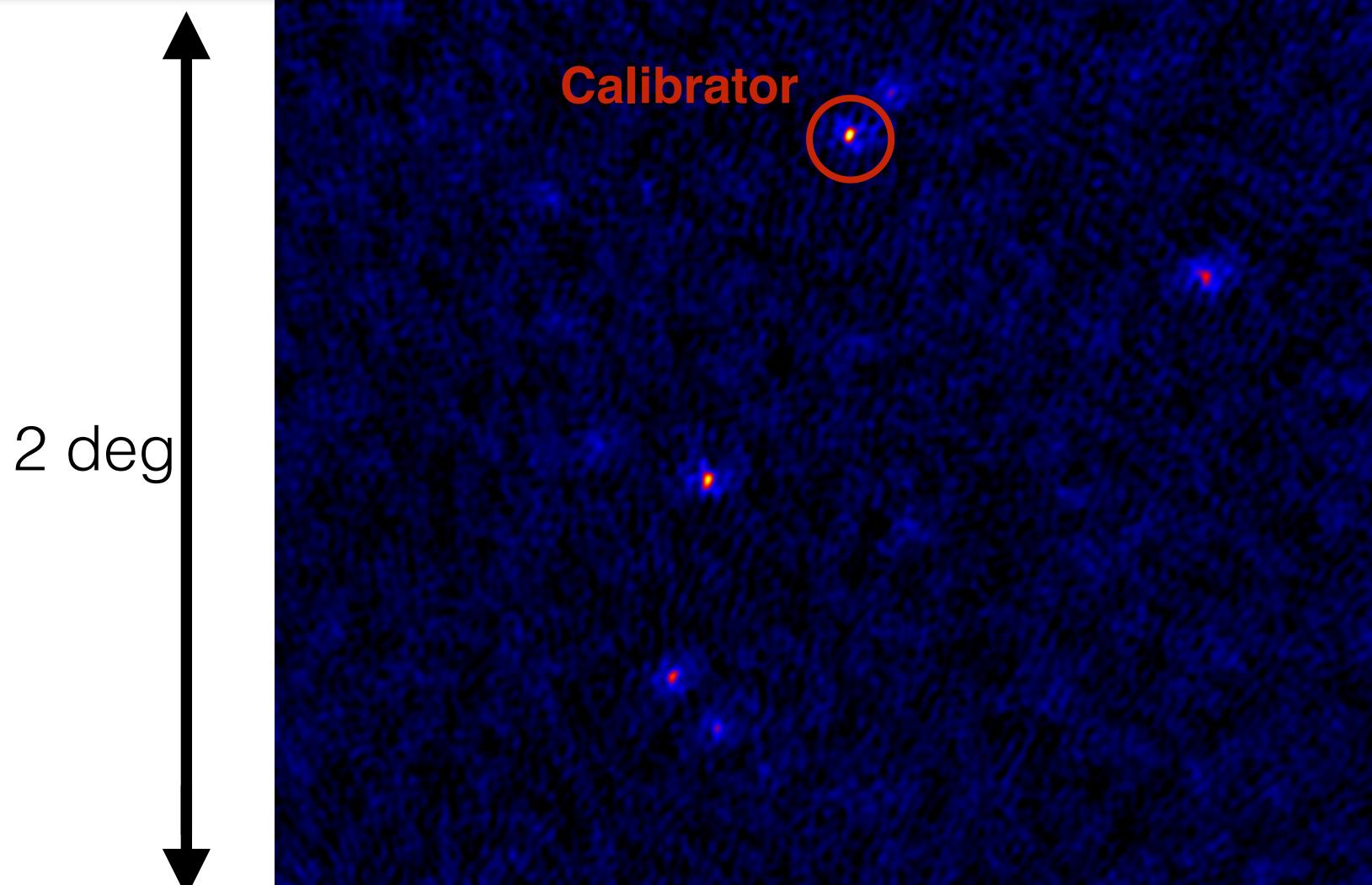
Source 2:

$$\phi_2^{\text{cal}} = \phi^{\text{instr}} + \phi_2^{\text{ion}}$$

$$\phi_1^{\text{cal}} - \phi_2^{\text{cal}} = \cancel{\phi^{\text{instr}}} + \phi_1^{\text{ion}} - \cancel{\phi^{\text{instr}}} - \phi_2^{\text{ion}}$$

- Test with MSSS (MVF) LBA data: 8 2-MHz bands, 9 11-minute snapshots

dTEC fitting: 30 MHz Images



Without phases screen

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CASA low-freq pipeline:

- EVLA, GMRT, LOFAR...
 - SPAM DD-calibration
 - Polarization-friendly
 - Wide-band

$G^+ = \begin{pmatrix} 0 & e^{ix} \\ 0 & 0 \end{pmatrix}; G^0 = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$
 $K^+ F^+ = e^{ix} R_{\text{eff}}(\theta); K^0 F^0 = e^{ix} \begin{pmatrix} 0 & e^{i\phi} \\ 0 & e^{-i\phi} \end{pmatrix}$
 $D^+ = EK(\theta, -\phi) R_{\text{eff}}(\theta); D^0 = R_{\text{eff}}(\theta) \begin{pmatrix} e^{i\phi} & 0 \\ 0 & e^{-i\phi} \end{pmatrix}$
 $\Rightarrow \underbrace{\begin{pmatrix} 0 & e^{ix} \\ 0 & 1 \end{pmatrix}}_{G^+} \underbrace{e^{ix} \underbrace{E K(\theta, -\phi) R_{\text{eff}}(\theta) R_{\text{eff}}(\theta) R_{\text{eff}}(Bx)}_{DF}}_{D^0} = \begin{pmatrix} e^{i\phi} & 0 \\ 0 & e^{-i\phi} \end{pmatrix}$
 $\Rightarrow \underbrace{\begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}}_{G^0} \underbrace{e^{ix} \underbrace{R_{\text{eff}}(\theta, -\phi) R_{\text{eff}}(\theta) R_{\text{eff}}(\theta) R_{\text{eff}}(Bx)}_{DF}}_{D^0} = \begin{pmatrix} \cos \phi & \sin \phi \\ -\sin \phi & \cos \phi \end{pmatrix}$
 $\vec{x}_i = \vec{H}_i - \vec{H} \quad t = t_i \quad \vec{x} = \vec{x}_i$
 $\text{TEC}(\vec{x}_i) \rightarrow \phi \text{ and } \vec{x} = \vec{x}_i$
 $\vec{V}^m = \vec{V}^m \uparrow \alpha K$
 $\vec{V}^m = D^{-1} G^{-1} V^m = F V^t$
 $\vec{X}^\phi = \frac{c}{v} \text{TEC}$
 $\vec{X}' = \frac{1}{2\pi} \frac{d\vec{X}^\phi}{dv} = -\frac{1}{2\pi v} \frac{c}{v} \text{TEC}$
 $\vec{X}' = \frac{-1}{2\pi v} \vec{X}^\phi$
 $\vec{X}^\phi = \sum_{n=1}^{\infty} \sum_{m=1}^{\infty} \sum_{i=1}^{\infty} \sum_{j=1}^{\infty} g_{ijnp} \vec{g}_{ip} \delta_{mj}$
 $\vec{X}' = \sum_{n=1}^{\infty} \sum_{m=1}^{\infty} \sum_{i=1}^{\infty} \sum_{j=1}^{\infty} g_{ijpn} \vec{g}_{ip} \delta_{mj}$
 $\vec{X}^\phi = \frac{c}{v^2} \text{BTEC}$
 $\vec{X}' = \frac{1}{2\pi} \frac{d\vec{X}^\phi}{dv} = -\frac{1}{2\pi v} \vec{X}^\phi$
 $\text{BTEC} = \beta \cdot \text{TEC}$
 $W_{ijpn} = \frac{1}{\sqrt{v_{ipn} + v_{jpn}^2}}$
 $W_{ijpn}^2 = \frac{1}{v_{ipn} + v_{jpn}^2}$
 $\text{coefs} = [S \times N_p + N_p \times 2 + 1]$

Ionosphere effect is:

- Time variable
 - Spatially coherent
 - Frequency dependent
 - Polarization dependent

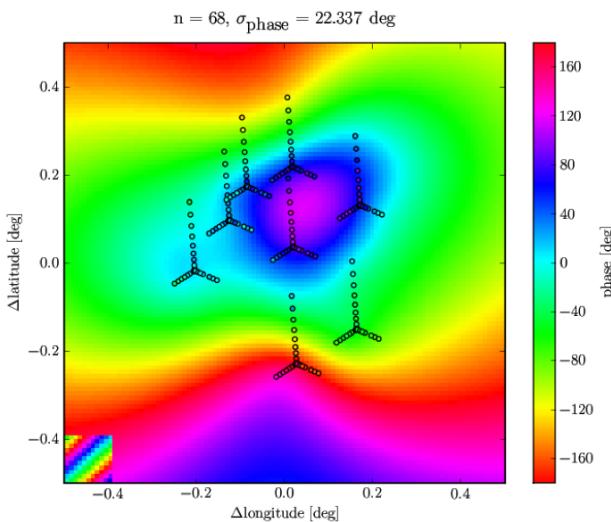
Instrumental effects are:

- Time constant
 - Spatially incoherent
 - Frequency independent
 - Polarization dependent
(different dependency of ionosphere)

CSPAM: linear polarisation

$$G = \begin{pmatrix} g_{xx} & 0 \\ 0 & g_{yy} \end{pmatrix}$$

Instrumental gain



$$KF = e^{i\chi} \text{Rot}(\beta\chi)$$

Ionosphere
(delay + Faraday rot.)

$$D = \text{Ell}(\theta, -\theta) \text{Rot}(\phi)$$

Leakage

Instrument Ionosphere

$$\begin{pmatrix} g_{xx} & 0 \\ 0 & g_{yy} \end{pmatrix} e^{i\chi} \text{Ell}(\theta, -\theta) \text{Rot}(\phi) \text{Rot}(\beta\chi)$$

Separation

- Ionosphere effect is:**
- Time variable
 - Spatially coherent
 - Frequency dependent
 - Polarisation dependent

Free parameters

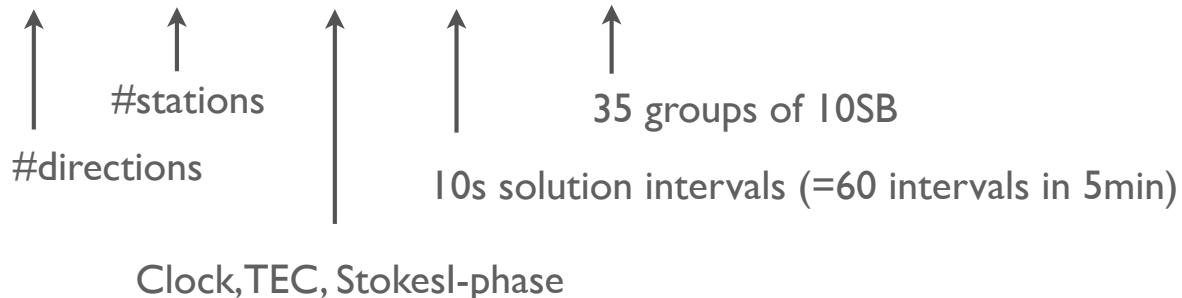
Full calibration:

$$100 \times 50 \times 350 \times 8 \text{ parameters} = 14\text{e}6 \text{ (1 sol interval: cannot track ionosphere)}$$



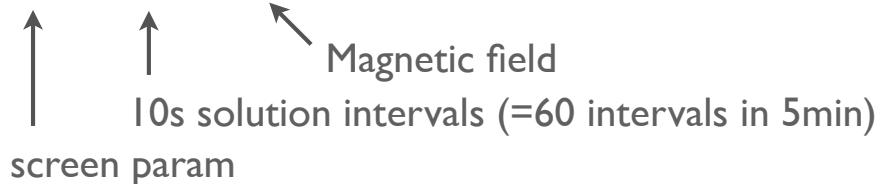
Extreme peeling:

$$100 \times 50 \times [(3 \times 60) + (35 \times 4)] = 1.6\text{e}6 \text{ (60 sol intervals: track ionosphere)}$$



TEC fitting:

$$5 \times 60 + 1 = 301 \text{ (60 sol intervals: track ionosphere)}$$



LoSoTo

Lofar Solutions Tool

RESET

PLOT: 1D/2D/TEC

SMOOTH: multidimensional smoothing

CLIP

ABS: absolute value

FLAG

NORM: normalize solutions

INTERP: interpolate solutions along (even multiple) axis.

TECFIT: fit TEC values to phase solutions

TECSCREEN: fit TEC screens to TEC values

CLOCKTEC: clock/tec separation.

EXAMPLE

*Check it in the LOFAR
imaging cookbook!*

Python



Developers
welcome!

<https://github.com/revoltek/losoto>